

# Package: marp (via r-universe)

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**Version** 0.1.0

**Type** Package

**Title** Model-Averaged Renewal Process

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**Description** To implement a model-averaging approach with different renewal models, with a primary focus on forecasting large earthquakes. Based on six renewal models (i.e., Poisson, Gamma, Log-Logistics, Weibull, Log-Normal and BPT), model-averaged point estimates are calculated using AIC (or BIC) weights. Additionally, both percentile and studentized bootstrapped model-averaged confidence intervals are constructed. In comparison, point and interval estimation from the individual or ``best" model (determined via model selection) can be retrieved.

**URL** <https://github.com/kanji709/marp>

**BugReports** <https://github.com/kanji709/marp/issues>

**Depends** R (>= 2.15)

**Imports** stats, gtools, statmod, VGAM,

**Suggests** knitr, devtools, roxygen2, testthat (>= 3.0.0)

**License** MIT + file LICENSE

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**NeedsCompilation** no

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bpt_bstrp	<i>A function to generate (double) bootstrap samples and fit BPT renewal model</i>
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### Description

A function to generate (double) bootstrap samples and fit BPT renewal model

### Usage

```
bpt_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)
```

**Arguments**

n	number of inter-event times
t	user-specified time intervals (used to compute hazard rate)
B	number of bootstrap samples
BB	number of double-bootstrap samples
m	the number of iterations in nlm
par_hat	estimated parameters
mu_hat	estimated mean inter-event times
pr_hat	estimated time to event probability
haz_hat	estimated hazard rates
y	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting BPT renewal model on (double) bootstrap samples, containing:

**mu\_star** Estimated mean from bootstrapped samples

**pr\_star** Estimated probability from bootstrapped samples

**haz\_star** Estimated hazard rates from bootstrapped samples

**mu\_var\_hat** Variance of estimated mean

**pr\_var\_hat** Variance of estimated probability

**haz\_var\_hat** Variance of estimated hazard rates

**mu\_var\_double** Variance of estimated mean of bootstrapped samples (via double-bootstrapping)

**pr\_var\_double** Variance of estimated probability of bootstrapped samples (via double-bootstrapping)

**haz\_var\_double** Variance of estimated hazard rates of bootstrapped samples (via double-bootstrapping)

**mu\_Tstar** Pivot quantity of the estimated mean

**pr\_Tstar** Pivot quantity of the estimated probability

**haz\_Tstar** Pivot quantity of the estimated hazard rates

**Examples**

```
# set some parameters
n <- 30 # sample size
t <- seq(100, 200, by = 10) # time intervals
B <- 100 # number of bootstraps
BB <- 100 # number of double-bootstraps
m <- 10 # number of iterations for MLE optimization
par_hat <- c(
  3.41361e-03, 2.76268e+00, 2.60370e+00, 3.30802e+02, 5.48822e+00, 2.92945e+02, NA,
  9.43071e-03, 2.47598e+02, 1.80102e+00, 6.50845e-01, 7.18247e-01
)
mu_hat <- c(292.94512, 292.94513, 319.72017, 294.16945, 298.87286, 292.94512)
pr_hat <- c(0.60039, 0.42155, 0.53434, 0.30780, 0.56416, 0.61795)
haz_hat <- matrix(c(
```

```

-5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -5.67999,
-5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -6.09420,
-5.99679, -5.91174, -5.83682, -5.77031, -5.71085, -5.65738,
-5.60904, -5.56512, -5.52504, -5.48833, -6.09902, -5.97017,
-5.85769, -5.75939, -5.67350, -5.59856, -5.53336, -5.47683,
-5.42805, -5.38621, -5.35060, -6.17146, -6.09512, -6.02542,
-5.96131, -5.90194, -5.84668, -5.79498, -5.74642, -5.70064,
-5.65733, -5.61624, -5.92355, -5.80239, -5.70475, -5.62524,
-5.55994, -5.50595, -5.46106, -5.42359, -5.39222, -5.36591,
-5.34383, -5.79111, -5.67660, -5.58924, -5.52166, -5.46879,
-5.42707, -5.39394, -5.36751, -5.34637, -5.32946, -5.31596
),length(t),6)
y <- 304 # cut-off point for probability estimation

# generate bootstrapped samples then fit renewal model
res <- marp::bpt_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)

```

---

bpt\_logl

*A function to calculate the log-likelihood of BPT model*


---

### Description

A function to calculate the log-likelihood of BPT model

### Usage

```
bpt_logl(param, x)
```

### Arguments

param	parameters of BPT model
x	input data for BPT model

### Value

returns the value of negative log-likelihood of the BPT model

### Examples

```

set.seed(42)
data <- rgamma(30,3,0.01)

# set some parameters
par_hat <- c(292.945125794581, 0.718247184450307) # estimated parameters
param <- c(log(par_hat[1]),log(par_hat[2]^2)) # input parameters for logl function

# calculate log-likelihood

```

```

result <- marp::bpt_logl(param, data)

# print result
cat("-logl = ", result, "\n")

```

---

bpt\_rp

*A function to fit BPT renewal model*


---

### Description

A function to fit BPT renewal model

### Usage

```
bpt_rp(data, t, m, y)
```

### Arguments

data	input inter-event times
t	user-specified time intervals (used to compute hazard rate)
m	the number of iterations in nlm
y	user-specified time point (used to compute time-to-event probability)

### Value

returns list of estimates after fitting BPT renewal model

**par1** Estimated parameter ( $\mu$ ) of the BPT model

**par2** Estimated parameter ( $\alpha$ ) of the BPT model

**logL** Negative log-likelihood

**AIC** Akaike information criterion (AIC)

**BIC** Bayesian information criterion (BIC)

**mu\_hat** Estimated mean

**pr\_hat** Estimated (logit) probabilities

**haz\_hat** Estimated (log) hazard rates

**Examples**

```

set.seed(42)
data <- rgamma(30,3,0.01)

# set some parameters
m <- 10 # number of iterations for MLE optimization
t <- seq(100, 200, by=10) # time intervals
y <- 304 # cut-off year for estimating probability

# fit BPT renewal model
result <- marp::bpt_rp(data, t, m, y)

# print result
cat("par1 = ", result$par1, "\n")
cat("par2 = ", result$par2, "\n")
cat("logL = ", result$logL, "\n")
cat("AIC = ", result$AIC, "\n")
cat("BIC = ", result$BIC, "\n")
cat("mu_hat = ", result$mu_hat, "\n")
cat("pr_hat = ", result$pr_hat, "\n")

```

---

dllog

*Density function of Log-Logistics model*


---

**Description**

Density function of Log-Logistics model

**Usage**

```
dllog(x, shape = 1, scale = 1, log = FALSE)
```

**Arguments**

x	input data for Log-Logistics model
shape	shape parameter of Log-Logistics model
scale	scale parameter of Log-Logistics model
log	logic function to determine whether log of logistics to be returned

**Value**

returns the density of the Log-Logistics model

**Examples**

```
x <- as.numeric(c(350., 450., 227., 352., 654.))
# set parameters
shape <- 5
scale <- 3
log <- FALSE
result_1 <- marp::dllog(x, shape, scale, log)

# alternatively, set log == TRUE
log <- TRUE
result_2 <- marp::dllog(x, shape, scale, log)
```

---

gamma_bstrp	<i>A function to generate (double) bootstrap samples and fit Gamma renewal model</i>
-------------	--

---

**Description**

A function to generate (double) bootstrap samples and fit Gamma renewal model

**Usage**

```
gamma_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)
```

**Arguments**

n	number of inter-event times
t	user-specified time intervals (used to compute hazard rate)
B	number of bootstrap samples
BB	number of double-bootstrap samples
m	the number of iterations in nlm
par_hat	estimated parameters
mu_hat	estimated mean inter-event times
pr_hat	estimated time to event probability
haz_hat	estimated hazard rates
y	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting Gamma renewal model on (double) bootstrap samples

**mu\_star** Estimated mean from bootstrapped samples

**pr\_star** Estimated probability from bootstrapped samples

**haz\_star** Estimated hazard rates from bootstrapped samples

**mu\_var\_hat** Variance of estimated mean  
**pr\_var\_hat** Variance of estimated probability  
**haz\_var\_hat** Variance of estimated hazard rates  
**mu\_var\_double** Variance of estimated mean of bootstrapped samples (via double-bootstrapping)  
**pr\_var\_double** Variance of estimated probability of bootstrapped samples (via double-bootstrapping)  
**haz\_var\_double** Variance of estimated hazard rates of bootstrapped samples (via double-bootstrapping)  
**mu\_Tstar** Pivot quantity of the estimated mean  
**pr\_Tstar** Pivot quantity of the estimated probability  
**haz\_Tstar** Pivot quantity of the estimated hazard rates

### Examples

```
# set some parameters
n <- 30 # sample size
t <- seq(100, 200, by = 10) # time intervals
B <- 100 # number of bootstraps
BB <- 100 # number of double-bootstraps
m <- 10 # number of iterations for MLE optimization
par_hat <- c(
  3.41361e-03, 2.76268e+00, 2.60370e+00, 3.30802e+02, 5.48822e+00, 2.92945e+02, NA,
  9.43071e-03, 2.47598e+02, 1.80102e+00, 6.50845e-01, 7.18247e-01
)
mu_hat <- c(292.94512, 292.94513, 319.72017, 294.16945, 298.87286, 292.94512)
pr_hat <- c(0.60039, 0.42155, 0.53434, 0.30780, 0.56416, 0.61795)
haz_hat <- matrix(c(
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -5.67999,
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -6.09420,
  -5.99679, -5.91174, -5.83682, -5.77031, -5.71085, -5.65738,
  -5.60904, -5.56512, -5.52504, -5.48833, -6.09902, -5.97017,
  -5.85769, -5.75939, -5.67350, -5.59856, -5.53336, -5.47683,
  -5.42805, -5.38621, -5.35060, -6.17146, -6.09512, -6.02542,
  -5.96131, -5.90194, -5.84668, -5.79498, -5.74642, -5.70064,
  -5.65733, -5.61624, -5.92355, -5.80239, -5.70475, -5.62524,
  -5.55994, -5.50595, -5.46106, -5.42359, -5.39222, -5.36591,
  -5.34383, -5.79111, -5.67660, -5.58924, -5.52166, -5.46879,
  -5.42707, -5.39394, -5.36751, -5.34637, -5.32946, -5.31596
),length(t),6)
y <- 304 # cut-off year for estimating probability

# generate bootstrapped samples then fit renewal model
res <- marp::gamma_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)
```



---

`gamma_logl`*A function to calculate the log-likelihood of Gamma model*

---

**Description**

A function to calculate the log-likelihood of Gamma model

**Usage**

```
gamma_logl(param, x)
```

**Arguments**

<code>param</code>	parameters of Gamma model
<code>x</code>	input data for Gamma model

**Value**

returns the value of negative log-likelihood of the Gamma model

**Examples**

```
set.seed(42)
data <- rgamma(30,3,0.01)

# set some parameters
par_hat <- c(2.7626793657057762, 0.0094307059277139432) # estimated parameters
param <- log(par_hat) # input parameters for logl function

# calculate log-likelihood
result <- marp::gamma_logl(param, data)

# print result
cat("-logl = ", result, "\n")
```

---

`gamma_rp`*A function to fit Gamma renewal model*

---

**Description**

A function to fit Gamma renewal model

**Usage**

```
gamma_rp(data, t, m, y)
```

**Arguments**

<code>data</code>	input inter-event times
<code>t</code>	user-specified time intervals (used to compute hazard rate)
<code>m</code>	the number of iterations in nlm
<code>y</code>	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting Gamma renewal model

**par1** Estimated shape parameter of the Gamma model

**par2** Estimated scale parameter of the Gamma model

**logL** Negative log-likelihood

**AIC** Akaike information criterion (AIC)

**BIC** Bayesian information criterion (BIC)

**mu\_hat** Estimated mean

**pr\_hat** Estimated (logit) probabilities

**haz\_hat** Estimated (log) hazard rates

**Examples**

```
set.seed(42)
data <- rgamma(100,3,0.01)

# set some parameters
m = 10 # number of iterations for MLE optimization
t = seq(100, 200, by=10) # time intervals
y = 304 # cut-off year for estimating probability

# fit Gamma renewal model
result <- marp::gamma_rp(data, t, m, y)

# print result
cat("par1 = ", result$par1, "\n")
cat("par2 = ", result$par2, "\n")
cat("logL = ", result$logL, "\n")
cat("AIC = ", result$AIC, "\n")
cat("BIC = ", result$BIC, "\n")
cat("mu_hat = ", result$mu_hat, "\n")
cat("pr_hat = ", result$pr_hat, "\n")
```

---

loglogis_bstrp	<i>A function to generate (double) bootstrap samples and fit Log-Logistic renewal model</i>
----------------	---

---

**Description**

A function to generate (double) bootstrap samples and fit Log-Logistic renewal model

**Usage**

```
loglogis_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)
```

**Arguments**

n	number of inter-event times
t	user-specified time intervals (used to compute hazard rate)
B	number of bootstrap samples
BB	number of double-bootstrap samples
m	the number of iterations in nlm
par_hat	estimated parameters
mu_hat	estimated mean inter-event times
pr_hat	estimated time to event probability
haz_hat	estimated hazard rates
y	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting Log-Logistic renewal model on (double) bootstrap samples

**mu\_star** Estimated mean from bootstrapped samples

**pr\_star** Estimated probability from bootstrapped samples

**haz\_star** Estimated hazard rates from bootstrapped samples

**mu\_var\_hat** Variance of estimated mean

**pr\_var\_hat** Variance of estimated probability

**haz\_var\_hat** Variance of estimated hazard rates

**mu\_var\_double** Variance of estimated mean of bootstrapped samples (via double-bootstrapping)

**pr\_var\_double** Variance of estimated probability of bootstrapped samples (via double-bootstrapping)

**haz\_var\_double** Variance of estimated hazard rates of bootstrapped samples (via double-bootstrapping)

**mu\_Tstar** Pivot quantity of the estimated mean

**pr\_Tstar** Pivot quantity of the estimated probability

**haz\_Tstar** Pivot quantity of the estimated hazard rates

**Examples**

```

# set some parameters
n <- 30 # sample size
t <- seq(100, 200, by = 10) # time intervals
B <- 100 # number of bootstraps
BB <- 100 # number of double-bootstraps
m <- 10 # number of iterations for MLE optimization
par_hat <- c(
  3.41361e-03, 2.76268e+00, 2.60370e+00, 3.30802e+02, 5.48822e+00, 2.92945e+02, NA,
  9.43071e-03, 2.47598e+02, 1.80102e+00, 6.50845e-01, 7.18247e-01
)
mu_hat <- c(292.94512, 292.94513, 319.72017, 294.16945, 298.87286, 292.94512)
pr_hat <- c(0.60039, 0.42155, 0.53434, 0.30780, 0.56416, 0.61795)
haz_hat <- matrix(c(
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -5.67999,
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -6.09420,
  -5.99679, -5.91174, -5.83682, -5.77031, -5.71085, -5.65738,
  -5.60904, -5.56512, -5.52504, -5.48833, -6.09902, -5.97017,
  -5.85769, -5.75939, -5.67350, -5.59856, -5.53336, -5.47683,
  -5.42805, -5.38621, -5.35060, -6.17146, -6.09512, -6.02542,
  -5.96131, -5.90194, -5.84668, -5.79498, -5.74642, -5.70064,
  -5.65733, -5.61624, -5.92355, -5.80239, -5.70475, -5.62524,
  -5.55994, -5.50595, -5.46106, -5.42359, -5.39222, -5.36591,
  -5.34383, -5.79111, -5.67660, -5.58924, -5.52166, -5.46879,
  -5.42707, -5.39394, -5.36751, -5.34637, -5.32946, -5.31596
),length(t),6)
y <- 304 # cut-off year for estimating probability

# generate bootstrapped samples then fit renewal model
res <- marp::loglogis_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)

```

---

loglogis\_logl

*A function to calculate the log-likelihood of Log-Logistics model*


---

**Description**

A function to calculate the log-likelihood of Log-Logistics model

**Usage**

```
loglogis_logl(param, x)
```

**Arguments**

param	parameters of Log-Logistics model
x	input data for Log-Logistics model

**Value**

returns the value of negative log-likelihood of the Log-Logistics model

**Examples**

```
set.seed(42)
data <- rgamma(30,3,0.01)

# set some parameters
par_hat <- c(2.6037079185931518, 247.59811806509711) # estimated parameters
param <- c(log(par_hat[2]),log(par_hat[1])) # input parameters for logl function

# calculate log-likelihood
result <- marp::loglogis_logl(param, data)

# print result
cat("-logl = ", result, "\n")
```

---

loglogis\_rp

*A function to fit Log-Logistics renewal model*


---

**Description**

A function to fit Log-Logistics renewal model

**Usage**

```
loglogis_rp(data, t, m, y)
```

**Arguments**

data	input inter-event times
t	user-specified time intervals (used to compute hazard rate)
m	the number of iterations in nlm
y	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting Log-Logistics renewal model

**par1** Estimated shape parameter of the Log-Logistics model

**par2** Estimated scale parameter of the Log-Logistics model

**logL** Negative log-likelihood

**AIC** Akaike information criterion (AIC)

**BIC** Bayesian information criterion (BIC)

**mu\_hat** Estimated mean  
**pr\_hat** Estimated (logit) probabilities  
**haz\_hat** Estimated (log) hazard rates

### Examples

```
set.seed(42)
data <- rgamma(100,3,0.01)

# set some parameters
m = 10 # number of iterations for MLE optimization
t = seq(100, 200, by=10) # time intervals
y = 304 # cut-off year for estimating probability

# fit Log-Logistic renewal model
result <- marp::loglogis_rp(data, t, m, y)

# print result
cat("par1 = ", result$par1, "\n")
cat("par2 = ", result$par2, "\n")
cat("logL = ", result$logL, "\n")
cat("AIC = ", result$AIC, "\n")
cat("BIC = ", result$BIC, "\n")
cat("mu_hat = ", result$mu_hat, "\n")
cat("pr_hat = ", result$pr_hat, "\n")
```

---

lognorm_bstrp	<i>A function to generate (double) bootstrap samples and fit Log-Normal renewal model</i>
---------------	---

---

### Description

A function to generate (double) bootstrap samples and fit Log-Normal renewal model

### Usage

```
lognorm_bstrp(n, t, B, BB, par_hat, mu_hat, pr_hat, haz_hat, y)
```

### Arguments

n	number of inter-event times
t	user-specified time intervals (used to compute hazard rate)
B	number of bootstrap samples
BB	number of double-bootstrap samples
par_hat	estimated parameters
mu_hat	estimated mean inter-event times

pr_hat	estimated time to event probability
haz_hat	estimated hazard rates
y	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting Log-Normal renewal model on (double) bootstrap samples

**mu\_star** Estimated mean from bootstrapped samples

**pr\_star** Estimated probability from bootstrapped samples

**haz\_star** Estimated hazard rates from bootstrapped samples

**mu\_var\_hat** Variance of estimated mean

**pr\_var\_hat** Variance of estimated probability

**haz\_var\_hat** Variance of estimated hazard rates

**mu\_var\_double** Variance of estimated mean of bootstrapped samples (via double-bootstrapping)

**pr\_var\_double** Variance of estimated probability of bootstrapped samples (via double-bootstrapping)

**haz\_var\_double** Variance of estimated hazard rates of bootstrapped samples (via double-bootstrapping)

**mu\_Tstar** Pivot quantity of the estimated mean

**pr\_Tstar** Pivot quantity of the estimated probability

**haz\_Tstar** Pivot quantity of the estimated hazard rates

**Examples**

```
# set some parameters
n <- 30 # sample size
t <- seq(100, 200, by = 10) # time intervals
B <- 100 # number of bootstraps
BB <- 100 # number of double-bootstraps
# m <- 10 # number of iterations for MLE optimization
par_hat <- c(
  3.41361e-03, 2.76268e+00, 2.60370e+00, 3.30802e+02, 5.48822e+00, 2.92945e+02, NA,
  9.43071e-03, 2.47598e+02, 1.80102e+00, 6.50845e-01, 7.18247e-01
)
mu_hat <- c(292.94512, 292.94513, 319.72017, 294.16945, 298.87286, 292.94512)
pr_hat <- c(0.60039, 0.42155, 0.53434, 0.30780, 0.56416, 0.61795)
haz_hat <- matrix(c(
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -5.67999,
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -6.09420,
  -5.99679, -5.91174, -5.83682, -5.77031, -5.71085, -5.65738,
  -5.60904, -5.56512, -5.52504, -5.48833, -6.09902, -5.97017,
  -5.85769, -5.75939, -5.67350, -5.59856, -5.53336, -5.47683,
  -5.42805, -5.38621, -5.35060, -6.17146, -6.09512, -6.02542,
  -5.96131, -5.90194, -5.84668, -5.79498, -5.74642, -5.70064,
  -5.65733, -5.61624, -5.92355, -5.80239, -5.70475, -5.62524,
  -5.55994, -5.50595, -5.46106, -5.42359, -5.39222, -5.36591,
  -5.34383, -5.79111, -5.67660, -5.58924, -5.52166, -5.46879,
  -5.42707, -5.39394, -5.36751, -5.34637, -5.32946, -5.31596
```

```

),length(t),6)
y <- 304 # cut-off year for estimating probablity

# generate bootstrapped samples then fit renewal model
res <- marp::lognorm_bstrp(n, t, B, BB, par_hat, mu_hat, pr_hat, haz_hat, y)

```

---

lognorm\_rp

*A function to fit Log-Normal renewal model*


---

### Description

A function to fit Log-Normal renewal model

### Usage

```
lognorm_rp(data, t, y)
```

### Arguments

<b>data</b>	as input inter-event times
<b>t</b>	as user-specified time intervals (used to compute hazard rate)
<b>y</b>	as user-specified time point (used to compute time-to-event probability)

### Value

returns list of estimates after fitting Log-Normal renewal model

**par1** Estimated mean (on the log scale) of the Log-Normal model

**par2** Estimated standard deviation (on the log scale)of the Log-Normal model

**logL** Negative log-likelihood

**AIC** Akaike information criterion (AIC)

**BIC** Bayesian information criterion (BIC)

**mu\_hat** Estimated mean

**pr\_hat** Estimated (logit) probabilities

**haz\_hat** Estimated (log) hazard rates



**Examples**

```

set.seed(42)
data <- rgamma(100,3,0.01)

# set some parameters
t = seq(100, 200, by=10) # time intervals
y = 304 # cut-off year for estimating probability

# fit Log-Normal renewal model
result <- marp::lognorm_rp(data, t, y)

# print result
cat("par1 = ", result$par1, "\n")
cat("par2 = ", result$par2, "\n")
cat("logL = ", result$logL, "\n")
cat("AIC = ", result$AIC, "\n")
cat("BIC = ", result$BIC, "\n")
cat("mu_hat = ", result$mu_hat, "\n")
cat("pr_hat = ", result$pr_hat, "\n")

```

---

lowerT

*An utility function to calculate upper limit of T statistic*


---

**Description**

An utility function to calculate upper limit of T statistic

**Usage**

```
lowerT(low, hat, sigmasq, Tstar, weights, B, alpha)
```

**Arguments**

low	lower limit
hat	estimates
sigmasq	variance
Tstar	T statistics estimated from bootstrap samples
weights	model weights
B	number of bootstraps
alpha	confidence level

**Value**

returns upper limit of T-statistic

**Examples**

```

# set some parameters
low <- 100 # lower bound
hat <- rep(150, 6) # estimates obtained from each model
sigmasq <- 10 # variance
Tstar <- matrix(rep(100,600),6,100) # T statistics estimated from bootstrap samples
weights <- rep(1/6, 6) # model weights
B <- 100 # number of bootstrapped samples
alpha <- 0.05 # confidence level

# calculate the upper limit of T statistics
res <- marp::lowerT(low, hat, sigmasq, Tstar, weights, B, alpha)

# print result
cat("res = ", res, "\n")

```

---

marp

*A function to apply model-averaged renewal process*


---

**Description**

A function to apply model-averaged renewal process

**Usage**

```
marp(data, t, m, y, which.model = 1)
```

**Arguments**

data	input inter-event times
t	user-specified time intervals (used to compute hazard rate)
m	the number of iterations in nlm
y	user-specified time point (used to compute time-to-event probability)
which.model	user-specified generating (or true underlying if known) model

**Value**

returns list of estimates obtained from different renewal processes and after applying model-averaging

**par1** Estimated scale parameters (if applicable) of all six renewal models

**par2** Estimated shape parameters (if applicable) of all six renewal models

**logL** Negative log-likelihood

**AIC** Akaike information criterion (AIC)

**BIC** Bayesian information criterion (BIC)

**mu\_hat** Estimated mean

**pr\_hat** Estimated (logit) probabilities  
**haz\_hat** Estimated (log) hazard rates  
**weights\_AIC** Model weights calculated based on AIC  
**weights\_BIC** Model weights calculated based on BIC  
**model\_best** Model selected based on the lowest AIC  
**mu\_best** Estimated mean obtained from the model with the lowest AIC  
**pr\_best** Estimated probability obtained from the model with the lowest AIC  
**haz\_best** Estimated hazard rates obtained from the model with the lowest AIC  
**mu\_gen** Estimated mean obtained from the (true or hypothetical) generating model  
**pr\_gen** Estimated probability obtained from the (true or hypothetical) generating model  
**haz\_gen** Estimated hazard rates obtained from the (true or hypothetical) generating model  
**mu\_aic** Estimated mean obtained from model-averaging (using AIC weights)  
**pr\_aic** Estimated probability obtained from model-averaging (using AIC weights)  
**haz\_aic** Estimated hazard rates obtained from model-averaging (using AIC weights)

### Examples

```

set.seed(42)
data <- rgamma(100,3,0.01)

# set some parameters
m = 10 # number of iterations for MLE optimization
t = seq(100, 200, by=10) # time intervals
y = 304 # cut-off year for estimating probability
which.model <- 2 # specify the generating model

# model selection and averaging
result <- marp::marp(data, t, m, y, which.model)
  
```

---

marp\_bstrp

*A function to fit model-averaged renewal process*


---

### Description

A function to fit model-averaged renewal process

### Usage

```
marp_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)
```

**Arguments**

n	number of inter-event times
t	user-specified time intervals (used to compute hazard rate)
B	number of bootstrap samples
BB	number of double-bootstrap samples
m	the number of iterations in nlm
par_hat	estimated parameters
mu_hat	estimated mean inter-event times
pr_hat	estimated time to event probability
haz_hat	estimated hazard rates
y	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting different renewal models on (double) bootstrap samples

**mu\_star** Estimated mean from bootstrapped samples

**pr\_star** Estimated probability from bootstrapped samples

**haz\_star** Estimated hazard rates from bootstrapped samples

**mu\_var\_hat** Variance of estimated mean

**pr\_var\_hat** Variance of estimated probability

**haz\_var\_hat** Variance of estimated hazard rates

**mu\_var\_double** Variance of estimated mean of bootstrapped samples (via double-bootstrapping)

**pr\_var\_double** Variance of estimated probability of bootstrapped samples (via double-bootstrapping)

**haz\_var\_double** Variance of estimated hazard rates of bootstrapped samples (via double-bootstrapping)

**mu\_Tstar** Pivot quantity of the estimated mean

**pr\_Tstar** Pivot quantity of the estimated probability

**haz\_Tstar** Pivot quantity of the estimated hazard rates

**Examples**

```
# set some parameters
n <- 30 # sample size
t <- seq(100, 200, by = 10) # time intervals
B <- 100 # number of bootstraps
BB <- 100 # number of double-bootstraps
m <- 10 # number of iterations for MLE optimization
par_hat <- c(
  3.41361e-03, 2.76268e+00, 2.60370e+00, 3.30802e+02, 5.48822e+00, 2.92945e+02, NA,
  9.43071e-03, 2.47598e+02, 1.80102e+00, 6.50845e-01, 7.18247e-01
)
mu_hat <- c(292.94512, 292.94513, 319.72017, 294.16945, 298.87286, 292.94512)
pr_hat <- c(0.60039, 0.42155, 0.53434, 0.30780, 0.56416, 0.61795)
haz_hat <- matrix(c(
```

```

-5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -5.67999,
-5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -6.09420,
-5.99679, -5.91174, -5.83682, -5.77031, -5.71085, -5.65738,
-5.60904, -5.56512, -5.52504, -5.48833, -6.09902, -5.97017,
-5.85769, -5.75939, -5.67350, -5.59856, -5.53336, -5.47683,
-5.42805, -5.38621, -5.35060, -6.17146, -6.09512, -6.02542,
-5.96131, -5.90194, -5.84668, -5.79498, -5.74642, -5.70064,
-5.65733, -5.61624, -5.92355, -5.80239, -5.70475, -5.62524,
-5.55994, -5.50595, -5.46106, -5.42359, -5.39222, -5.36591,
-5.34383, -5.79111, -5.67660, -5.58924, -5.52166, -5.46879,
-5.42707, -5.39394, -5.36751, -5.34637, -5.32946, -5.31596
),length(t),6)
y <- 304 # cut-off year for estimating probablity

# generate bootstrapped samples then fit renewal model
res <- marp::marp_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)

```

---

marp\_confint

*A function to apply model-averaged renewal process*


---

## Description

A function to apply model-averaged renewal process

## Usage

```
marp_confint(data, m, t, B, BB, alpha, y, which.model)
```

## Arguments

data	input inter-event times
m	the number of iterations in nlm
t	user-specified time intervals (used to compute hazard rate)
B	number of bootstrap samples
BB	number of double-bootstrap samples
alpha	significance level
y	user-specified time point (used to compute time-to-event probability)
which.model	user-specified generating (or true underlying if known) model

## Value

returns list of point and interval estimation obtained from different renewal models (including model-averaged confidence intervals).

**par1** Estimated scale parameters (if applicable) of all six renewal models

**par2** Estimated shape parameters (if applicable) of all six renewal models

**logL** Negative log-likelihood

**AIC** Akaike information criterion (AIC)

**BIC** Bayesian information criterion (BIC)

**mu\_hat** Estimated mean

**pr\_hat** Estimated (logit) probabilities

**haz\_hat** Estimated (log) hazard rates

**weights\_AIC** Model weights calculated based on AIC

**weights\_BIC** Model weights calculated based on BIC

**model\_best** Model selected based on the lowest AIC

**mu\_best** Estimated mean obtained from the model with the lowest AIC

**pr\_best** Estimated probability obtained from the model with the lowest AIC

**haz\_best** Estimated hazard rates obtained from the model with the lowest AIC

**mu\_gen** Estimated mean obtained from the (true or hypothetical) generating model

**pr\_gen** Estimated probability obtained from the (true or hypothetical) generating model

**haz\_gen** Estimated hazard rates obtained from the (true or hypothetical) generating model

**mu\_aic** Estimated mean obtained from model-averaging (using AIC weights)

**pr\_aic** Estimated probability obtained from model-averaging (using AIC weights)

**haz\_aic** Estimated hazard rates obtained from model-averaging (using AIC weights)

**mu\_bstrp** Estimated mean obtained from model-averaging (using bootstrapped weights)

**pr\_bstrp** Estimated probability obtained from model-averaging (using bootstrapped weights)

**haz\_bstrp** Estimated hazard rates obtained from model-averaging (using bootstrapped weights)

**weights\_bstp** Model weights calculated by bootstrapping, that is, the frequency of each model being selected as the best model is divided by the total number of bootstraps

**mu\_gen** Median of the percentile bootstrap confidence interval of the estimated mean based on the generating model

**mu\_gen\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated mean based on the generating model

**mu\_gen\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated mean based on the generating model

**mu\_best** Median of the percentile bootstrap confidence interval of the estimated mean based on the best model

**mu\_best\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated mean based on the best model

**mu\_best\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated mean based on the best model

**pr\_gen** Median of the percentile bootstrap confidence interval of the estimated probabilities based on the generating model

**pr\_gen\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated probabilities based on the generating model

- pr\_gen\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated probabilities based on the generating model
- pr\_best** Median of the percentile bootstrap confidence interval of the estimated probabilities based on the best model
- pr\_best\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated probabilities based on the best model
- pr\_best\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated probabilities based on the best model
- haz\_gen** Median of the percentile bootstrap confidence interval of the estimated hazard rates based on the generating model
- haz\_gen\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated hazard rates based on the generating model
- haz\_gen\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated hazard rates based on the generating model
- haz\_best** Median of the percentile bootstrap confidence interval of the estimated hazard rates based on the best model
- haz\_best\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated hazard rates based on the best model
- haz\_best\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated hazard rates based on the best model
- mu\_lower\_gen** Lower limit of the studentized bootstrap confidence interval of the estimated mean based on the generating model
- mu\_upper\_gen** Upper limit of the studentized bootstrap confidence interval of the estimated mean based on the generating model
- mu\_lower\_best** Lower limit of the studentized bootstrap confidence interval of the estimated mean based on the best model
- mu\_upper\_best** Upper limit of the studentized bootstrap confidence interval of the estimated mean based on the best model
- pr\_lower\_gen** Lower limit of the studentized bootstrap confidence interval of the estimated probabilities based on the generating model
- pr\_upper\_gen** Upper limit of the studentized bootstrap confidence interval of the estimated probabilities based on the generating model
- pr\_lower\_best** Lower limit of the studentized bootstrap confidence interval of the estimated probabilities based on the best model
- pr\_upper\_best** Upper limit of the studentized bootstrap confidence interval of the estimated probabilities based on the best model
- haz\_lower\_gen** Lower limit of the studentized bootstrap confidence interval of the estimated hazard rates based on the generating model
- haz\_upper\_gen** Upper limit of the studentized bootstrap confidence interval of the estimated hazard rates based on the generating model
- haz\_lower\_best** Lower limit of the studentized bootstrap confidence interval of the estimated hazard rates based on the best model

**haz\_upper\_best** Upper limit of the studentized bootstrap confidence interval of the estimated hazard rates based on the best model

**mu\_lower\_ma** Lower limit of model-averaged studentized bootstrap confidence interval of the estimated mean

**mu\_upper\_ma** Upper limit of model-averaged studentized bootstrap confidence interval of the estimated mean

**pr\_lower\_ma** Lower limit of model-averaged studentized bootstrap confidence interval of the estimated probabilities

**pr\_upper\_ma** Upper limit of model-averaged studentized bootstrap confidence interval of the estimated probabilities

**haz\_lower\_ma** Lower limit of model-averaged studentized bootstrap confidence interval of the estimated hazard rates

**haz\_upper\_ma** Upper limit of model-averaged studentized bootstrap confidence interval of the estimated hazard rates

## Examples

```
# generate random data
set.seed(42)
data <- rgamma(30, 3, 0.01)

# set some parameters
m <- 10 # number of iterations for MLE optimization
t <- seq(100,200,by=10) # time intervals
alpha <- 0.05 # confidence level
y <- 304 # cut-off year for estimating probability
B <- 100 # number of bootstraps
BB <- 100 # number of double bootstraps
which.model <- 2 # specify the generating model

# construct confidence intervals
res <- marp::marp_confint(data,m,t,B,BB,alpha,y,which.model)
```

---

percent\_confint

*A function to calculate percentile bootstrap confidence interval*

---

## Description

A function to calculate percentile bootstrap confidence interval

## Usage

```
percent_confint(data, B, t, m, y, which.model = 1)
```



**Arguments**

<code>data</code>	input inter-event times
<code>B</code>	number of bootstrap samples
<code>t</code>	user-specified time intervals (used to compute hazard rate)
<code>m</code>	the number of iterations in nlm
<code>y</code>	user-specified time point (used to compute time-to-event probability)
<code>which.model</code>	user-specified generating (or true underlying if known) model

**Value**

returns list of percentile bootstrap intervals (including the model-averaged approach).

**weights\_bstp** Model weights calculated by bootstrapping, that is, the frequency of each model being selected as the best model is divided by the total number of bootstraps

**mu\_gen** Median of the percentile bootstrap confidence interval of the estimated mean based on the generating model

**mu\_gen\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated mean based on the generating model

**mu\_gen\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated mean based on the generating model

**mu\_best** Median of the percentile bootstrap confidence interval of the estimated mean based on the best model

**mu\_best\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated mean based on the best model

**mu\_best\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated mean based on the best model

**pr\_gen** Median of the percentile bootstrap confidence interval of the estimated probabilities based on the generating model

**pr\_gen\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated probabilities based on the generating model

**pr\_gen\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated probabilities based on the generating model

**pr\_best** Median of the percentile bootstrap confidence interval of the estimated probabilities based on the best model

**pr\_best\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated probabilities based on the best model

**pr\_best\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated probabilities based on the best model

**haz\_gen** Median of the percentile bootstrap confidence interval of the estimated hazard rates based on the generating model

**haz\_gen\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated hazard rates based on the generating model

**haz\_gen\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated hazard rates based on the generating model

**haz\_best** Median of the percentile bootstrap confidence interval of the estimated hazard rates based on the best model

**haz\_best\_lower** Lower limit of the percentile bootstrap confidence interval of the estimated hazard rates based on the best model

**haz\_best\_upper** Upper limit of the percentile bootstrap confidence interval of the estimated hazard rates based on the best model

### Examples

```
# generate random data
set.seed(42)
data <- rgamma(30, 3, 0.01)

# set some parameters
m <- 10 # number of iterations for MLE optimization
t <- seq(100,200,by=10) # time intervals
y <- 304 # cut-off year for estimating probability
B <- 100 # number of bootstraps
BB <- 100 # number of double bootstraps
which.model <- 2 # specify the generating model

# construct percentile bootstrap confidence intervals
marp::percent_confint(data, B, t, m, y, which.model)
```

---

pllog

*Probability function of Log-Logistics model*

---

### Description

Probability function of Log-Logistics model

### Usage

```
pllog(q, shape = 1, scale = 1, lower.tail = TRUE, log.p = FALSE)
```

### Arguments

q	input quantile for Log-Logistics model
shape	shape parameter of Log-Logistics model
scale	scale parameter of Log-Logistics model
lower.tail	logic function to determine whether lower tail probability to be returned
log.p	logic function to determine whether log of logistics to be returned

**Value**

returns the probability of the Log-Logistics model

**Examples**

```
q <- c(1, 2, 3, 4)
# set paramters
shape <- 5
scale <- 3
log <- FALSE
result_1 <- marp::pllog(q, shape, scale, log)

# alternatively, set log == TRUE
log <- TRUE
result_2 <- marp::pllog(q, shape, scale, log)
```

---

poisson_bstrp	<i>A function to generate (double) bootstrap samples and fit Poisson renewal model</i>
---------------	--

---

**Description**

A function to generate (double) bootstrap samples and fit Poisson renewal model

**Usage**

```
poisson_bstrp(n, t, B, BB, par_hat, mu_hat, pr_hat, haz_hat, y)
```

**Arguments**

n	number of inter-event times
t	user-specified time intervals (used to compute hazard rate)
B	number of bootstrap samples
BB	number of double-bootstrap samples
par_hat	estimated parameters
mu_hat	estimated mean inter-event times
pr_hat	estimated time to event probability
haz_hat	estimated hazard rates
y	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting Poisson renewal model on (double) bootstrap samples

**mu\_star** Estimated mean from bootstrapped samples

**pr\_star** Estimated probability from bootstrapped samples

**haz\_star** Estimated hazard rates from bootstrapped samples

**mu\_var\_hat** Variance of estimated mean

**pr\_var\_hat** Variance of estimated probability

**haz\_var\_hat** Variance of estimated hazard rates

**mu\_var\_double** Variance of estimated mean of bootstrapped samples (via double-bootstrapping)

**pr\_var\_double** Variance of estimated probability of bootstrapped samples (via double-bootstrapping)

**haz\_var\_double** Variance of estimated hazard rates of bootstrapped samples (via double-bootstrapping)

**mu\_Tstar** Pivot quantity of the estimated mean

**pr\_Tstar** Pivot quantity of the estimated probability

**haz\_Tstar** Pivot quantity of the estimated hazard rates

**Examples**

```
# set some parameters
n <- 30 # sample size
t <- seq(100, 200, by = 10) # time intervals
B <- 100 # number of bootstraps
BB <- 100 # number of double-bootstraps
# m <- 10 # number of iterations for MLE optimization
par_hat <- c(
  3.41361e-03, 2.76268e+00, 2.60370e+00, 3.30802e+02, 5.48822e+00, 2.92945e+02, NA,
  9.43071e-03, 2.47598e+02, 1.80102e+00, 6.50845e-01, 7.18247e-01
)
mu_hat <- c(292.94512, 292.94513, 319.72017, 294.16945, 298.87286, 292.94512)
pr_hat <- c(0.60039, 0.42155, 0.53434, 0.30780, 0.56416, 0.61795)
haz_hat <- matrix(c(
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -5.67999,
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -6.09420,
  -5.99679, -5.91174, -5.83682, -5.77031, -5.71085, -5.65738,
  -5.60904, -5.56512, -5.52504, -5.48833, -6.09902, -5.97017,
  -5.85769, -5.75939, -5.67350, -5.59856, -5.53336, -5.47683,
  -5.42805, -5.38621, -5.35060, -6.17146, -6.09512, -6.02542,
  -5.96131, -5.90194, -5.84668, -5.79498, -5.74642, -5.70064,
  -5.65733, -5.61624, -5.92355, -5.80239, -5.70475, -5.62524,
  -5.55994, -5.50595, -5.46106, -5.42359, -5.39222, -5.36591,
  -5.34383, -5.79111, -5.67660, -5.58924, -5.52166, -5.46879,
  -5.42707, -5.39394, -5.36751, -5.34637, -5.32946, -5.31596
),length(t),6)
y <- 304 # cut-off year for estimating probability

# generate bootstrapped samples then fit renewal model
res <- marp::poisson_bstrp(n, t, B, BB, par_hat, mu_hat, pr_hat, haz_hat, y)
```

---

poisson\_rp                      *A function to fit Poisson renewal model*

---

### Description

A function to fit Poisson renewal model

### Usage

```
poisson_rp(data, t, y)
```

### Arguments

data	input inter-event times
t	user-specified time intervals (used to compute hazard rate)
y	user-specified time point (used to compute time-to-event probability)

### Value

returns list of estimates after fitting Poisson renewal model

**par1** Estimated parameter of the Poisson model

**par2** N/A, only keep it as a place holder for output formatting purpose

**logL** Negative log-likelihood

**AIC** Akaike information criterion (AIC)

**BIC** Bayesian information criterion (BIC)

**mu\_hat** Estimated mean

**pr\_hat** Estimated (logit) probabilities

**haz\_hat** Estimated (log) hazard rates

### Examples

```
set.seed(42)
data <- rgamma(100,3,0.01)

# set some parameters
t = seq(100, 200, by=10) # time intervals
y = 304 # cut-off year for estimating probablity

# fit Poisson renewal model
result <- marp::poisson_rp(data, t, y)

# print result
cat("par1 = ", result$par1, "\n")
cat("par2 = ", result$par2, "\n")
cat("logL = ", result$logL, "\n")
```

```

cat("AIC = ", result$AIC, "\n")
cat("BIC = ", result$BIC, "\n")
cat("mu_hat = ", result$mu_hat, "\n")
cat("pr_hat = ", result$pr_hat, "\n")

```

---

student_confint	<i>A function to calculate Studentized bootstrap confidence interval</i>
-----------------	--

---

### Description

A function to calculate Studentized bootstrap confidence interval

### Usage

```

student_confint(
  n,
  B,
  t,
  m,
  BB,
  par_hat,
  mu_hat,
  pr_hat,
  haz_hat,
  weights,
  alpha,
  y,
  best.model,
  which.model = 1
)

```

### Arguments

n	number of inter-event times
B	number of bootstrap samples
t	user-specified time intervals (used to compute hazard rate)
m	the number of iterations in nlm
BB	number of double-bootstrap samples
par_hat	estimated parameters
mu_hat	estimated mean inter-event times
pr_hat	estimated time to event probability
haz_hat	estimated hazard rates
weights	model weights

alpha	significance level
y	user-specified time point (used to compute time-to-event probability)
best.model	best model based on information criterion (i.e. AIC)
which.model	user-specified generating (or true underlying if known) model

**Value**

returns list of Studentized bootstrap intervals (including the model-averaged approach).

**mu\_lower\_gen** Lower limit of the studentized bootstrap confidence interval of the estimated mean based on the generating model

**mu\_upper\_gen** Upper limit of the studentized bootstrap confidence interval of the estimated mean based on the generating model

**mu\_lower\_best** Lower limit of the studentized bootstrap confidence interval of the estimated mean based on the best model

**mu\_upper\_best** Upper limit of the studentized bootstrap confidence interval of the estimated mean based on the best model

**pr\_lower\_gen** Lower limit of the studentized bootstrap confidence interval of the estimated probabilities based on the generating model

**pr\_upper\_gen** Upper limit of the studentized bootstrap confidence interval of the estimated probabilities based on the generating model

**pr\_lower\_best** Lower limit of the studentized bootstrap confidence interval of the estimated probabilities based on the best model

**pr\_upper\_best** Upper limit of the studentized bootstrap confidence interval of the estimated probabilities based on the best model

**haz\_lower\_gen** Lower limit of the studentized bootstrap confidence interval of the estimated hazard rates based on the generating model

**haz\_upper\_gen** Upper limit of the studentized bootstrap confidence interval of the estimated hazard rates based on the generating model

**haz\_lower\_best** Lower limit of the studentized bootstrap confidence interval of the estimated hazard rates based on the best model

**haz\_upper\_best** Upper limit of the studentized bootstrap confidence interval of the estimated hazard rates based on the best model

**mu\_lower\_ma** Lower limit of model-averaged studentized bootstrap confidence interval of the estimated mean

**mu\_upper\_ma** Upper limit of model-averaged studentized bootstrap confidence interval of the estimated mean

**pr\_lower\_ma** Lower limit of model-averaged studentized bootstrap confidence interval of the estimated probabilities

**pr\_upper\_ma** Upper limit of model-averaged studentized bootstrap confidence interval of the estimated probabilities

**haz\_lower\_ma** Lower limit of model-averaged studentized bootstrap confidence interval of the estimated hazard rates

**haz\_upper\_ma** Upper limit of model-averaged studentized bootstrap confidence interval of the estimated hazard rates

**Examples**

```

# generate random data
set.seed(42)
data <- rgamma(30, 3, 0.01)

# set some parameters
n <- 30 # sample size
m <- 10 # number of iterations for MLE optimization
t <- seq(100,200,by=10) # time intervals
y <- 304 # cut-off year for estimating probablilty
B <- 100 # number of bootstraps
BB <- 100 # number of double bootstraps
par_hat <- c(
  3.41361e-03, 2.76268e+00, 2.60370e+00, 3.30802e+02, 5.48822e+00, 2.92945e+02, NA,
  9.43071e-03, 2.47598e+02, 1.80102e+00, 6.50845e-01, 7.18247e-01)
mu_hat <- c(292.94512, 292.94513, 319.72017, 294.16945, 298.87286, 292.94512)
pr_hat <- c(0.60039, 0.42155, 0.53434, 0.30780, 0.56416, 0.61795)
haz_hat <- matrix(c(
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -5.67999,
  -5.67999, -5.67999, -5.67999, -5.67999, -5.67999, -6.09420,
  -5.99679, -5.91174, -5.83682, -5.77031, -5.71085, -5.65738,
  -5.60904, -5.56512, -5.52504, -5.48833, -6.09902, -5.97017,
  -5.85769, -5.75939, -5.67350, -5.59856, -5.53336, -5.47683,
  -5.42805, -5.38621, -5.35060, -6.17146, -6.09512, -6.02542,
  -5.96131, -5.90194, -5.84668, -5.79498, -5.74642, -5.70064,
  -5.65733, -5.61624, -5.92355, -5.80239, -5.70475, -5.62524,
  -5.55994, -5.50595, -5.46106, -5.42359, -5.39222, -5.36591,
  -5.34383, -5.79111, -5.67660, -5.58924, -5.52166, -5.46879,
  -5.42707, -5.39394, -5.36751, -5.34637, -5.32946, -5.31596
),length(t),6)
weights <- c(0.00000, 0.21000, 0.02000, 0.55000, 0.00000, 0.22000) # model weights
alpha <- 0.05 # confidence level
y <- 304 # cut-off year for estimating probablilty
best.model <- 2
which.model <- 2 # specify the generating model#'

# construct Studentized bootstrap confidence interval
marp::student_confint(
  n,B,t,m,BB,par_hat,mu_hat,pr_hat,haz_hat,weights,alpha,y,best.model,which.model
)

```

---

upperT

---

*An utility function to calculate lower limit of T statistic*


---

**Description**

An utility function to calculate lower limit of T statistic



**Usage**

```
upperT(up, hat, sigmasq, Tstar, weights, B, alpha)
```

**Arguments**

up	upper limit
hat	estimates
sigmasq	variance
Tstar	T statistics estimated from bootstrap samples
weights	model weights
B	number of bootstraps
alpha	confidence level

**Value**

returns lower limit of T statistic

**Examples**

```
# set some parameters
up <- 100 # upper bound
hat <- rep(150, 6) # estimates obtained from each model
sigmasq <- 10 # variance
Tstar <- matrix(rep(100,600),6,100) # T statistics estimated from bootstrap samples
weights <- rep(1/6, 6) # model weights
B <- 100 # number of bootstrapped samples
alpha <- 0.05 # confidence level

# calculate the upper limit of T statistics
res <- marp::upperT(up, hat, sigmasq, Tstar, weights, B, alpha)

# print result
cat("res = ", res, "\n")
```

---

weibull_bstrp	<i>A function to generate (double) bootstrap samples and fit Weibull renewal model</i>
---------------	--

---

**Description**

A function to generate (double) bootstrap samples and fit Weibull renewal model

**Usage**

```
weibull_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)
```

**Arguments**

n	number of inter-event times
t	user-specified time intervals (used to compute hazard rate)
B	number of bootstrap samples
BB	number of double-bootstrap samples
m	the number of iterations in nlm
par_hat	estimated parameters
mu_hat	estimated mean inter-event times
pr_hat	estimated time to event probability
haz_hat	estimated hazard rates
y	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting Weibull renewal model on (double) bootstrap samples

**mu\_star** Estimated mean from bootstrapped samples

**pr\_star** Estimated probability from bootstrapped samples

**haz\_star** Estimated hazard rates from bootstrapped samples

**mu\_var\_hat** Variance of estimated mean

**pr\_var\_hat** Variance of estimated probability

**haz\_var\_hat** Variance of estimated hazard rates

**mu\_var\_double** Variance of estimated mean of bootstrapped samples (via double-bootstrapping)

**pr\_var\_double** Variance of estimated probability of bootstrapped samples (via double-bootstrapping)

**haz\_var\_double** Variance of estimated hazard rates of bootstrapped samples (via double-bootstrapping)

**mu\_Tstar** Pivot quantity of the estimated mean

**pr\_Tstar** Pivot quantity of the estimated probability

**haz\_Tstar** Pivot quantity of the estimated hazard rates

**Examples**

```
# set some parameters
n <- 30 # sample size
t <- seq(100, 200, by = 10) # time intervals
B <- 100 # number of bootstraps
BB <- 100 # number of double-bootstraps
m <- 10 # number of iterations for MLE optimization
par_hat <- c(
  3.4136086430979953e-03, 2.7626793657057762e+00, 2.6037039674870583e+00, 3.3080162440951688e+02,
  5.4882183788378658e+00, 2.9294512422957860e+02, NA, 9.4307059277139432e-03,
  2.4759796859031687e+02, 1.8010183507666513e+00, 6.5084541680686814e-01, 7.1824719073918109e-01
)
mu_hat <- c(
  292.94512187913182, 292.94512912200048, 319.72017228620746, 294.16945213908519,
```

```

298.87285747700128, 292.94512422957860
)
pr_hat <- c(
  0.60038574701819891, 0.42154974433034809, 0.53433568234281148, 0.30779792692414687,
  0.56416103510057725, 0.61794524610544410
)
haz_hat <- matrix(c(
  -5.6799852941338829, -5.6799852941338829, -5.6799852941338829, -5.6799852941338829,
  -5.6799852941338829, -5.6799852941338829, -5.6799852941338829, -5.6799852941338829,
  -5.6799852941338829, -5.6799852941338829, -5.6799852941338829, -6.0942031084732298,
  -5.9967873794574516, -5.9117418563554684, -5.8368230853439300, -5.7703089176306639,
  -5.7108525626839901, -5.6573839062669986, -5.6090408956082456, -5.5651206740587922,
  -5.5250440506799734, -5.4883291920475745, -6.0990192429336094, -5.9701664705134210,
  -5.8576899644670348, -5.7593884711134971, -5.6734972529860741, -5.5985621349393231,
  -5.5333565788683616, -5.4768259914915305, -5.4280496904694857, -5.3862145095364315,
  -5.3505961502861927, -6.1714638710963881, -6.0951186680582552, -6.0254209583640863,
  -5.9613052806725335, -5.9019434350392981, -5.8466788789061646, -5.7949823391436279,
  -5.7464209045603756, -5.7006359661738628, -5.6573271297614109, -5.6162402596857071,
  -5.9235521978533958, -5.8023896004395645, -5.7047473880293342, -5.6252373537796752,
  -5.5599409055534252, -5.5059486025117375, -5.4610610586440487, -5.4235891601883868,
  -5.3922173604047572, -5.3659081375131672, -5.3438339586221275, -5.7911126719889303,
  -5.6765973314326752, -5.5892417143301261, -5.5216608261560411, -5.4687921205249133,
  -5.4270729562323066, -5.3939387902533049, -5.3675067327627373, -5.3463701567645607,
  -5.3294619641245422, -5.3159614865560094
),length(t),6)
y <- 304 # cut-off year for estimating probablity

# generate bootstrapped samples then fit renewal model
res <- marp::weibull_bstrp(n, t, B, BB, m, par_hat, mu_hat, pr_hat, haz_hat, y)

```

---

weibull\_logl

*A function to calculate the log-likelihood of Weibull model*


---

## Description

A function to calculate the log-likelihood of Weibull model

## Usage

```
weibull_logl(param, x)
```

## Arguments

param	parameters of Weibull model
x	input data for Weibull model

**Value**

returns the value of negative log-likelihood of the Weibull model

**Examples**

```
set.seed(42)
data <- rgamma(30,3,0.01)

# set some parameters
par_hat <- c(330.801103808081, 1.8010133877944) # estimated parameters
param <- log(par_hat) # input parameters for logl function

# calculate log-likelihood
result <- marp::weibull_logl(param, data)

# print result
cat("-logl = ", result, "\n")
```

---

weibull\_rp

*A function to fit Weibull renewal model #' @import weibull\_logl*


---

**Description**

A function to fit Weibull renewal model #' @import weibull\_logl

**Usage**

```
weibull_rp(data, t, m, y)
```

**Arguments**

data	input inter-event times
t	user-specified time intervals (used to compute hazard rate)
m	the number of iterations in nlm
y	user-specified time point (used to compute time-to-event probability)

**Value**

returns list of estimates after fitting Weibull renewal model

**par1** Estimated scale parameter of the Weibull model

**par2** Estimated shape parameter of the Weibull model

**logL** Negative log-likelihood

**AIC** Akaike information criterion (AIC)

**BIC** Bayesian information criterion (BIC)

**mu\_hat** Estimated mean

**pr\_hat** Estimated (logit) probabilities

**haz\_hat** Estimated (log) hazard rates

### Examples

```
set.seed(42)
data <- rgamma(100,3,0.01)

# set some parameters
m = 10 # number of iterations for MLE optimization
t = seq(100, 200, by=10) # time intervals
y = 304 # cut-off year for estimating probability

# fit Weibull renewal model
result <- marp::weibull_rp(data, t, m, y)

# print result
cat("par1 = ", result$par1, "\n")
cat("par2 = ", result$par2, "\n")
cat("logL = ", result$logL, "\n")
cat("AIC = ", result$AIC, "\n")
cat("BIC = ", result$BIC, "\n")
cat("mu_hat = ", result$mu_hat, "\n")
cat("pr_hat = ", result$pr_hat, "\n")
```

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