

# Package: finbipartite (via r-universe)

February 28, 2025

**Title** Learning Bipartite Graphs: Heavy Tails and Multiple Components

**Version** 0.1.0

**Date** 2023-02-02

**Description** Learning bipartite and k-component bipartite graphs from financial datasets. This package contains implementations of the algorithms described in the paper: Cardoso JVM, Ying J, and Palomar DP (2022). <<https://openreview.net/pdf?id=WNSyF9qZaMd>> ``Learning bipartite graphs: heavy tails and multiple components, Advances in Neural Informations Processing Systems" (NeurIPS).

**URL** <https://github.com/convexfi/bipartite/>

**BugReports** <https://github.com/convexfi/bipartite/issues>

**License** GPL-3

**Encoding** UTF-8

**Depends** spectralGraphTopology, quadprog

**Imports** MASS, stats, progress, mvtnorm, CVXR

**Suggests** testthat, igraph,

**RoxygenNote** 7.1.1

**NeedsCompilation** no

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**Config/pak/sysreqs** libgmp3-dev make libxml2-dev libmpfr-dev

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### learn\_bipartite\_graph\_nie

*Laplacian matrix of a k-component bipartite graph via Nie's method  
Computes the Laplacian matrix of a bipartite graph on the basis of an observed similarity matrix.*

## Description

Laplacian matrix of a k-component bipartite graph via Nie's method  
Computes the Laplacian matrix of a bipartite graph on the basis of an observed similarity matrix.

## Usage

```
learn_bipartite_graph_nie(
  S,
  r,
  q,
  k,
  learning_rate = 1e-04,
  eta = 1,
  maxiter = 1000,
  reltol = 1e-06,
  verbose = TRUE,
  record_objective = FALSE
)
```

## Arguments

S	a p x p similarity matrix, where p is the number of nodes in the graph.
r	number of nodes in the objects set.
q	number of nodes in the classes set.
k	number of components of the graph.
learning_rate	gradient descent parameter.
eta	rank constraint hyperparameter.
maxiter	maximum number of iterations.
reltol	relative tolerance as a convergence criteria.

verbose	whether or not to show a progress bar during the iterations.
record_objective	whether or not to record the objective function value during iterations.

**Value**

A list containing possibly the following elements:

laplacian	estimated Laplacian matrix
adjacency	estimated adjacency matrix
B	estimated graph weights matrix
maxiter	number of iterations taken to reach convergence
convergence	boolean flag to indicate whether or not the optimization converged
obj_fun	objective function value per iteration

**References**

Feiping Nie, Xiaoqian Wang, Cheng Deng, Heng Huang. "Learning A Structured Optimal Bipartite Graph for Co-Clustering". Advances in Neural Information Processing Systems (NIPS 2017)

**Examples**

```

library(fnbipartite)
library(igraph)
set.seed(42)
r <- 50
q <- 5
p <- r + q

bipartite <- sample_bipartite(r, q, type="Gnp", p = 1, directed=FALSE)
# randomly assign edge weights to connected nodes
E(bipartite)$weight <- 1
Lw <- as.matrix(laplacian_matrix(bipartite))
B <- -Lw[1:r, (r+1):p]
B[,] <- runif(length(B))
B <- B / rowSums(B)
# utils functions
from_B_to_laplacian <- function(B) {
  A <- from_B_to_adjacency(B)
  return(diag(rowSums(A)) - A)
}

from_B_to_adjacency <- function(B) {
  r <- nrow(B)
  q <- ncol(B)
  zeros_rxr <- matrix(0, r, r)
  zeros_qxq <- matrix(0, q, q)
  return(rbind(cbind(zeros_rxr, B), cbind(t(B), zeros_qxq)))
}
Ltrue <- from_B_to_laplacian(B)

```

```
X <- MASS::mvrnorm(100*p, rep(0, p), MASS::ginv(Ltrue))
S <- cov(X)
bipartite_graph <- learn_bipartite_graph_nie(S = S,
                                              r = r,
                                              q = q,
                                              k = 1,
                                              learning_rate = 5e-1,
                                              eta = 0,
                                              verbose=FALSE)
```

**learn\_connected\_bipartite\_graph\_pgd**

*Laplacian matrix of a connected bipartite graph with Gaussian data  
Computes the Laplacian matrix of a bipartite graph on the basis of an  
observed data matrix.*

**Description**

Laplacian matrix of a connected bipartite graph with Gaussian data

Computes the Laplacian matrix of a bipartite graph on the basis of an observed data matrix.

**Usage**

```
learn_connected_bipartite_graph_pgd(
  S,
  r,
  q,
  init = "naive",
  learning_rate = 1e-04,
  maxiter = 1000,
  reltol = 1e-05,
  verbose = TRUE,
  record_objective = FALSE,
  backtrack = TRUE
)
```

**Arguments**

S	a p x p covariance matrix, where p is the number of nodes in the graph.
r	number of nodes in the objects set.
q	number of nodes in the classes set.
init	string denoting how to compute the initial graph.
learning_rate	gradient descent parameter.
maxiter	maximum number of iterations.
reltol	relative tolerance as a convergence criteria.

verbose	whether or not to show a progress bar during the iterations.
record_objective	whether or not to record the objective function value during iterations.
backtrack	whether or not to optimize the learning rate via backtracking.

### Value

A list containing possibly the following elements:

laplacian	estimated Laplacian matrix
adjacency	estimated adjacency matrix
B	estimated graph weights matrix
maxiter	number of iterations taken to reach convergence
convergence	boolean flag to indicate whether or not the optimization converged
lr_seq	learning rate value per iteration
obj_seq	objective function value per iteration
elapsed_time	time taken per iteration until convergence is reached

### Examples

```

library(fbinbipartite)
library(igraph)
set.seed(42)
r <- 50
q <- 5
p <- r + q

bipartite <- sample_bipartite(r, q, type="Gnp", p = 1, directed=FALSE)
# randomly assign edge weights to connected nodes
E(bipartite)$weight <- 1
Lw <- as.matrix(laplacian_matrix(bipartite))
B <- -Lw[1:r, (r+1):p]
B[,] <- runif(length(B))
B <- B / rowSums(B)
# utils functions
from_B_to_laplacian <- function(B) {
  A <- from_B_to_adjacency(B)
  return(diag(rowSums(A)) - A)
}

from_B_to_adjacency <- function(B) {
  r <- nrow(B)
  q <- ncol(B)
  zeros_rxr <- matrix(0, r, r)
  zeros_qxq <- matrix(0, q, q)
  return(rbind(cbind(zeros_rxr, B), cbind(t(B), zeros_qxq)))
}
Ltrue <- from_B_to_laplacian(B)
X <- MASS::mvrnorm(100*p, rep(0, p), MASS::ginv(Ltrue))

```

```
S <- cov(X)
bipartite_graph <- learn_connected_bipartite_graph_pgd(S = S,
                                                       r = r,
                                                       q = q,
                                                       verbose=FALSE)
```

**learn\_heavy\_tail\_bipartite\_graph\_pgd**

*Laplacian matrix of a connected bipartite graph with heavy-tailed data* Computes the Laplacian matrix of a bipartite graph on the basis of an observed data matrix whose distribution is assumed to be Student-t.

**Description**

Laplacian matrix of a connected bipartite graph with heavy-tailed data

Computes the Laplacian matrix of a bipartite graph on the basis of an observed data matrix whose distribution is assumed to be Student-t.

**Usage**

```
learn_heavy_tail_bipartite_graph_pgd(
  X,
  r,
  q,
  nu = 2.001,
  learning_rate = 1e-04,
  maxiter = 1000,
  reltol = 1e-05,
  init = "default",
  verbose = TRUE,
  record_objective = FALSE,
  backtrack = TRUE
)
```

**Arguments**

X	a n x p data matrix, where p is the number of nodes in the graph and n is the number of observations.
r	number of nodes in the objects set.
q	number of nodes in the classes set.
nu	degrees of freedom of the Student-t distribution.
learning_rate	gradient descent parameter.
maxiter	maximum number of iterations.
reltol	relative tolerance as a convergence criteria.

init	string denoting how to compute the initial graph or a r x q matrix with initial graph weights.
verbose	whether or not to show a progress bar during the iterations.
record_objective	whether or not to record the objective function value during iterations.
backtrack	whether or not to optimize the learning rate via backtracking.

## Value

A list containing possibly the following elements:

laplacian	estimated Laplacian matrix
adjacency	estimated adjacency matrix
B	estimated graph weights matrix
maxiter	number of iterations taken to reach convergence
convergence	boolean flag to indicate whether or not the optimization converged
lr_seq	learning rate value per iteration
obj_seq	objective function value per iteration
elapsed_time	time taken per iteration until convergence is reached

## Examples

```

library(fnbipartite)
library(igraph)
set.seed(42)
r <- 50
q <- 5
p <- r + q

bipartite <- sample_bipartite(r, q, type="Gnp", p = 1, directed=FALSE)
# randomly assign edge weights to connected nodes
E(bipartite)$weight <- 1
Lw <- as.matrix(laplacian_matrix(bipartite))
B <- -Lw[1:r, (r+1):p]
B[, ] <- runif(length(B))
B <- B / rowSums(B)
# utils functions
from_B_to_laplacian <- function(B) {
  A <- from_B_to_adjacency(B)
  return(diag(rowSums(A)) - A)
}

from_B_to_adjacency <- function(B) {
  r <- nrow(B)
  q <- ncol(B)
  zeros_rxr <- matrix(0, r, r)
  zeros_qxq <- matrix(0, q, q)
  return(rbind(cbind(zeros_rxr, B), cbind(t(B), zeros_qxq)))
}

```

```

}
Ltrue <- from_B_to_laplacian(B)
X <- MASS::mvrnorm(100*p, rep(0, p), MASS::ginv(Ltrue))
bipartite_graph <- learn_heavy_tail_bipartite_graph_pgd(X = X,
                                                       r = r,
                                                       q = q,
                                                       nu = 1e2,
                                                       verbose=FALSE)

```

### learn\_heavy\_tail\_kcomp\_bipartite\_graph

*Laplacian matrix of a k-component bipartite graph with heavy-tailed data*  
*Computes the Laplacian matrix of a k-component bipartite graph on the basis of an observed data matrix whose distribution is assumed to be Student-t.*

### Description

Laplacian matrix of a k-component bipartite graph with heavy-tailed data

Computes the Laplacian matrix of a k-component bipartite graph on the basis of an observed data matrix whose distribution is assumed to be Student-t.

### Usage

```

learn_heavy_tail_kcomp_bipartite_graph(
  X,
  r,
  q,
  k,
  nu = 2.001,
  rho = 1,
  learning_rate = 1e-04,
  maxiter = 1000,
  reltol = 1e-05,
  init = "default",
  verbose = TRUE,
  record_objective = FALSE
)

```

### Arguments

X	a n x p data matrix, where p is the number of nodes in the graph and n is the number of observations.
r	number of nodes in the objects set.
q	number of nodes in the classes set.
k	number of components of the graph.

nu	degrees of freedom of the Student-t distribution.
rho	ADMM hyperparameter.
learning_rate	gradient descent parameter.
maxiter	maximum number of iterations.
reltol	relative tolerance as a convergence criteria.
init	string denoting how to compute the initial graph or a r x q matrix with initial graph weights.
verbose	whether or not to show a progress bar during the iterations.
record_objective	whether or not to record the objective function value during iterations.

## Value

A list containing possibly the following elements:

laplacian	estimated Laplacian matrix
adjacency	estimated adjacency matrix
B	estimated graph weights matrix
maxiter	number of iterations taken to reach convergence
convergence	boolean flag to indicate whether or not the optimization converged
dual_residual	dual residual value per iteration
primal_residual	primal residual value per iteration
aug_lag	augmented Lagrangian value per iteration
rho_seq	constraint relaxation hyperparameter value per iteration
elapsed_time	time taken per iteration until convergence is reached

## Examples

```

library(finbipartite)
library(igraph)
set.seed(42)
r <- 50
q <- 5
p <- r + q

bipartite <- sample_bipartite(r, q, type="Gnp", p = 1, directed=FALSE)
# randomly assign edge weights to connected nodes
E(bipartite)$weight <- 1
Lw <- as.matrix(laplacian_matrix(bipartite))
B <- -Lw[1:r, (r+1):p]
B[,] <- runif(length(B))
B <- B / rowSums(B)
# utils functions
from_B_to_laplacian <- function(B) {
  A <- from_B_to_adjacency(B)
}

```

```
return(diag(rowSums(A)) - A)
}

from_B_to_adjacency <- function(B) {
  r <- nrow(B)
  q <- ncol(B)
  zeros_rxr <- matrix(0, r, r)
  zeros_qxq <- matrix(0, q, q)
  return(rbind(cbind(zeros_rxr, B), cbind(t(B), zeros_qxq)))
}
Ltrue <- from_B_to_laplacian(B)
X <- MASS::mvrnorm(100*p, rep(0, p), MASS::ginv(Ltrue))
bipartite_graph <- learn_heavy_tail_kcomp_bipartite_graph(X = X,
  r = r,
  q = q,
  k = 1,
  nu = 1e2,
  verbose=FALSE)
```

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