Package: cxhull (via r-universe)

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Type Package

Title Convex Hull

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Description Computes the convex hull in arbitrary dimension, based on the Qhull library (<http://www.qhull.org>). The package provides a complete description of the convex hull: edges, ridges, facets, adjacencies. Triangulation is optional.

License GPL-3

URL https://github.com/stla/cxhull

BugReports https://github.com/stla/cxhull/issues

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Imports data.table, grDevices, rgl, Rvcg

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cxhull

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Convex hull

Description

Computes the convex hull of a set of points.

Usage

cxhull(points, triangulate = FALSE)

Arguments

points	numeric matrix, one point per row
triangulate	logical, whether to triangulate the convex hull

Value

A list providing a lot of information about the convex hull. See the **README** file for details.

```
library(cxhull)
points <- rbind(
    c(0.5,0.5,0.5),
    c(0,0,0),
    c(0,0,1),
    c(0,1,0),
    c(0,1,1),
    c(1,0,0),
    c(1,0,1),
    c(1,1,0),</pre>
```

cxhullEdges

c(1,1,1)
)
cxhull(points)

cxhullEdges Vertices and edges of convex hull

Description

Computes the vertices and the edges of the convex hull of a set of points.

Usage

```
cxhullEdges(points, adjacencies = FALSE, orderEdges = FALSE)
```

Arguments

points	numeric matrix, one point per row; it must contain at least three columns (the two-dimensional case is not implemented yet)
adjacencies	Boolean, whether to return the vertex adjacencies
orderEdges	Boolean, whether to order the edges in the output

Value

A list with two fields: vertices and edges. The vertices field is a list which provides an id for each vertex and its coordinates. If adjacencies=TRUE, it provides in addition the ids of the adjacent vertices for each vertex. The edges fields is an integer matrix with two columns. Each row provides the two ids of the vertices of the corresponding edge.

```
library(cxhull)
# let's try with the hexacosichoron (see `?hexacosichoron`)
# it is convex so its convex hull is itself
VE <- cxhullEdges(hexacosichoron)</pre>
edges <- VE[["edges"]]</pre>
random_edge <- edges[sample.int(720L, 1L), ]</pre>
A <- hexacosichoron[random_edge[1L], ]</pre>
B <- hexacosichoron[random_edge[2L], ]</pre>
sqrt(c(crossprod(A - B))) # this is 2/phi
# Now let's project the polytope to the H4 Coxeter plane
phi <- (1 + sqrt(5)) / 2
u1 <- c(
  0,
  2*phi*sin(pi/30),
  0,
  1
)
u2 <- c(
```

```
2*phi*sin(pi/15),
  0.
  2*sin(2*pi/15),
  0
)
u1 <- u1 / sqrt(c(crossprod(u1)))</pre>
u2 <- u2 / sqrt(c(crossprod(u2)))</pre>
# projections to the Coxeter plane
proj <- function(v){</pre>
  c(c(crossprod(v, u1)), c(crossprod(v, u2)))
}
points <- t(apply(hexacosichoron, 1L, proj))</pre>
# we will assign a color to each edge
# according to the norms of its two vertices
norms2 <- round(apply(points, 1L, crossprod), 1L)</pre>
( tbl <- table(norms2) )</pre>
#> 0.4 1.6 2.4 3.6
#> 30 30 30 30
values <- as.numeric(names(tbl))</pre>
grd <- as.matrix(expand.grid(values, values))</pre>
grd <- grd[grd[, 1L] <= grd[, 2L], ]</pre>
pairs <- apply(grd, 1L, paste0, collapse = "-")</pre>
colors <- hcl.colors(nrow(grd), palette = "Hawaii", rev = TRUE)</pre>
if(require("colorspace")) {
  colors <- colorspace::darken(colors, amount = 0.3)</pre>
}
names(colors) <- pairs</pre>
# plot ####
opar <- par(mar = c(0, 0, 0, 0))
plot(
  points[!duplicated(points), ], pch = 19, cex = 0.3, asp = 1,
  axes = FALSE, xlab = NA, ylab = NA
)
for(i in 1L:nrow(edges)){
  twopoints <- points[edges[i, ], ]</pre>
  nrms2 <- round(sort(apply(twopoints, 1L, crossprod)), 1L)</pre>
  pair <- paste0(nrms2, collapse = "-")</pre>
  lines(twopoints, lwd = 0.5, col = colors[pair])
}
par(opar)
```

daVinciSphere Leonardo da Vinci's 72-sided sphere

Description

A matrix giving the 62 vertices of da Vinci's 72-sided sphere, a convex polyhedra with 72 faces.

Usage

daVinciSphere

dihedralAngles

Format

A matrix with 62 rows and 3 columns.

Source

http://www.matematicasvisuales.com/english/html/geometry/space/sphereCampanus.html

dihedralAngles Dihedral angles

Description

Dihedral angles of a convex hull.

Usage

```
dihedralAngles(hull)
```

Arguments

hull

an output of cxhull applied to 3D points

Value

A dataframe with three columns. The two first columns represent the edges, given as a pair of vertex indices. The third column provides the dihedral angle in degrees corresponding to the edge, that is the angle between the two faces incident to this edge. This is useful to find edges between two coplanar faces: if the faces are exactly coplanar then the dihedral angle is 180, but because of numerical approximation one can consider that there is coplanarity when the dihedral angle is greater than 179, for example. This function is used in plotConvexHull3d to get rid of such edges (if the user sets a value to the argument angleThreshold).

```
# a cube ####
library(cxhull)
points <- rbind(
    c(0.5,0.5,0.5),
    c(0,0,0),
    c(0,0,1),
    c(0,1,0),
    c(0,1,1),
    c(1,0,0),
    c(1,0,1),
    c(1,1,0),
    c(1,1,1)
)
hull <- cxhull(points)
dihedralAngles(hull)</pre>
```

EdgesAB

Description

Edges of a triangulated 3D convex hull given by the ids of the vertices in a matrix, plus a column indicating the border edges.

Usage

EdgesAB(hull)

Arguments

hull

an output of cxhull applied to 3D points and with the option triangulate=TRUE

Value

A character matrix with three columns. Each row provides the ids of the two vertices of an edge, and a yes/no indicator of whether the edge is a border edge.

```
library(cxhull)
library(rgl)
dodecahedron <- t(dodecahedron3d()$vb[-4L, ])</pre>
hull <- cxhull(dodecahedron, triangulate = TRUE)</pre>
triangles <- TrianglesXYZ(hull)</pre>
triangles3d(triangles, color = "yellow")
edges <- EdgesAB(hull)</pre>
trueEdges <- edges[edges[, 3L] == "yes", c(1L, 2L)]</pre>
otherEdges <- edges[edges[, 3L] == "no", c(1L, 2L)]</pre>
vertices <- VerticesXYZ(hull)</pre>
for(i in 1:nrow(trueEdges)){
  lines3d(vertices[trueEdges[i, ], ], color = "blue", lwd = 3)
}
for(i in 1:nrow(otherEdges)){
  lines3d(vertices[otherEdges[i, ], ], color = "red", lwd = 3)
}
```

EdgesXYZ

Description

The coordinates of the extremities of the edges in a matrix, plus a column indicating which edges are border edges.

Usage

```
EdgesXYZ(hull)
```

Arguments

hull an output of cxhull applied to 3D points and with the option triangulate=TRUE

Value

A numeric matrix with four columns. The first three values of a row are the coordinates of a vertex at the extremity of an edge, and the fourth column indicates whether the edge is a border edge.

hexacosichoron Vertices of the 600-cell

Description

A matrix giving the 120 vertices of the hexacosichoron, a regular convex 4D polytope also known as the "600-cell", with edge length 2/phi, where phi is the golden number. It has 720 edges.

Usage

hexacosichoron

Format

A matrix with 120 rows and 4 columns.

Source

https://www.qfbox.info/4d/600-cell

hullMesh

Description

Extract the vertices and the faces from a 3d convex hull.

Usage

hullMesh(hull, simplify = TRUE, rgl = FALSE)

Arguments

hull	a 3d convex hull, output of cxhull
simplify	Boolean, whether to return the faces as a matrix instead of a list if possible, i.e. if all faces have the same number of edges; this argument is possibly ignored if rgl=TRUE, see below
rgl	Boolean, whether to return a rgl mesh (class mesh3d) if possible, i.e. if each face has three or four edges; if TRUE and the rgl mesh is possible, then the simplify argument has no effect

Value

A list giving the vertices and the faces, or a **rgl** mesh.

Note

Unless all faces are triangular, the output does not define a mesh with coherently oriented faces.

```
library(cxhull)
hull <- cxhull(daVinciSphere)
septuaginta <- hullMesh(hull, rgl = TRUE)
library(rgl)
open3d(windowRect = c(50, 50, 562, 562))
shade3d(septuaginta, color = "darkred")
# some quad faces are misoriented:
open3d(windowRect = c(50, 50, 562, 562))
shade3d(septuaginta, color = "tomato", back = "culled")
```

hullSummary

Description

Summary of a triangulated 3D convex hull

Usage

```
hullSummary(hull)
```

Arguments

hull an output of cxhull applied to 3D points and with the option triangulate=TRUE

Value

A list with the vertices and the facets.

Examples

```
library(cxhull)
# pyramid
pts <- rbind(
    c(0, 0, 0),
    c(1, 0, 0),
    c(1, 1, 0),
    c(0.5, 0.5, 1),
    c(0.5, 0.5, 0.9),
    c(0, 1, 0)
)
hull <- cxhull(pts, triangulate = TRUE)
hullSummary(hull)</pre>
```

plotConvexHull3d Plot triangulated 3d convex hull

Description

Plot a triangulated 3d convex hull with rgl.

Usage

```
plotConvexHull3d(
 hull,
 angleThreshold = NULL,
 edgesAsTubes = TRUE,
 verticesAsSpheres = TRUE,
 palette = NULL,
 bias = 1,
  interpolate = "linear",
 g = identity,
 facesColor = "navy",
 edgesColor = "gold",
  tubesRadius = 0.03,
  spheresRadius = 0.05,
  spheresColor = edgesColor,
 alpha = 1
)
```

Arguments

hull	an output of ${\tt cxhull}$ applied to 3d points and with the option ${\tt triangulate=TRUE}$		
angleThreshold	a threshold angle in degrees, typically 179, to get rid of edges between coplanar faces: edges whose corresponding dihedral angle is greater than this threshold are removed; NULL to use another method (see the Leonardo example)		
edgesAsTubes	Boolean, whether to draw the edges as tubes		
verticesAsSpheres			
	Boolean, whether to draw the vertices as spheres		
palette	a vector of colors to make a color gradient for the faces; if NULL, the colors of the faces are controlled by the facesColor argument		
bias, interpolat	e		
	if palette is not NULL, these arguments are passed to colorRamp		
g	a function defined on $[0, 1]$ and taking its values in $[0, 1]$; it is composed with the function created by colorRamp, based on palette		
facesColor	the color(s) for the faces; this argument is ignored if the argument palette is not NULL; otherwise there are three possibilities for facesColor: a single color, a vector of colors with length the number of triangles, in which case one color is assigned per triangle, or a vector of colors with length the number of faces, after merging the triangles, in which case one color is assigned per face; use hullSummary to know the number of faces		
edgesColor	the color for the edges		
tubesRadius	the radius of the tubes when edgesAsTubes=TRUE		
spheresRadius	the radius of the spheres when verticesAsSpheres=TRUE		
spheresColor	the color of the spheres when verticesAsSpheres=TRUE		
alpha	number between 0 and 1 controlling the opacity of the faces		

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TrianglesXYZ

Value

No value.

Examples

```
library(cxhull)
library(rgl)
cuboctahedron <- t(cuboctahedron3d()$vb[-4L, ])</pre>
hull <- cxhull(cuboctahedron, triangulate = TRUE)</pre>
# single color ####
open3d(windowRect = c(50, 50, 562, 562))
plotConvexHull3d(hull)
# gradient ####
open3d(windowRect = c(50, 50, 562, 562))
if(getRversion() < "4.1.0"){
  palette <- "Viridis"</pre>
}else{
  palette <- "Rocket"</pre>
}
plotConvexHull3d(hull, palette = hcl.colors(256, palette), bias = 0.5)
library(cxhull)
library(rgl)
# Leonardo da Vinci's 72-sided sphere ####
hull <- cxhull(daVinciSphere, triangulate = TRUE)</pre>
# there are some undesirable edges:
plotConvexHull3d(
  hull, tubesRadius = 0.07, spheresRadius = 0.1
)
# => use `angleThreshold` to get rid of these edges:
plotConvexHull3d(
  hull, angleThreshold = 179,
  tubesRadius = 0.07, spheresRadius = 0.1
)
```

TrianglesXYZ Triangles of a triangulated 3D convex hull

Description

Coordinates of the vertices of the triangles of a triangulated 3D convex hull.

Usage

TrianglesXYZ(hull)

Arguments

hull an output of cxhull applied to 3D points and with the option triangulate=TRUE

Value

A matrix with three columns. Each row represents the coordinates of a vertex of a triangle.

Examples

```
library(cxhull)
library(rgl)
dodecahedron <- t(dodecahedron3d()$vb[-4L, ])
hull <- cxhull(dodecahedron, triangulate = TRUE)
triangles <- TrianglesXYZ(hull)
triangles3d(triangles, color = "firebrick")</pre>
```

VerticesXYZ

Convex hull vertices

Description

The coordinates of the vertices of a 3D convex hull.

Usage

```
VerticesXYZ(hull)
```

Arguments

hull an output of cxhull applied to 3D points

Value

A matrix with three columns. Each row represents the coordinates of a vertex and the row names are the ids of the vertices.

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