

Package: OwenQ (via r-universe)

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Type Package

Title Owen Q-Function

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Description Evaluates the Owen Q-function for an integer value of the degrees of freedom, by applying Owen's algorithm (1965) <[doi:10.1093/biomet/52.3-4.437](https://doi.org/10.1093/biomet/52.3-4.437)>. It is useful for the calculation of the power of equivalence tests.

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URL <https://github.com/stla/OwenQ>

BugReports <https://github.com/stla/OwenQ/issues>

Imports Rcpp (>= 0.12.10), stats

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VignetteBuilder knitr

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Additional_repositories <https://cranhaven.r-universe.dev>

Repository <https://cranhaven.r-universe.dev>

RemoteUrl <https://github.com/cranhaven/cranhaven.r-universe.dev>

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OwenQ1	<i>First Owen Q-function</i>
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Description

Evaluates the first Owen Q-function (integral from 0 to R) for an integer value of the degrees of freedom.

Usage

```
OwenQ1(nu, t, delta, R, algo = 2)
```

Arguments

nu	integer greater than 1, the number of degrees of freedom
t	number, positive or negative, possibly infinite
delta	vector of finite numbers, with the same length as R
R	(upper bound of the integral) vector of finite positive numbers, with the same length as delta
algo	the algorithm, 1 or 2

Value

A vector of numbers between 0 and 1, the values of the integral from 0 to R .

Note

When the number of degrees of freedom is odd, the procedure resorts to the Owen T-function ([OwenT](#)).

References

Owen, D. B. (1965). A special case of a bivariate noncentral t-distribution. *Biometrika* **52**, 437-446.

Examples

```
# As R goes to Inf, OwenQ1(nu, t, delta, R) goes to pt(t, nu, delta):
OwenQ1(nu=5, t=3, delta=2, R=100)
pt(q=3, df=5, ncp=2)
```

OwenQ2

Second Owen Q-function

Description

Evaluates the second Owen Q-function (integral from R to ∞) for an integer value of the degrees of freedom.

Usage

```
OwenQ2(nu, t, delta, R, algo = 2)
```

Arguments

nu	integer greater than 1, the number of degrees of freedom
t	number, positive or negative, possibly infinite
delta	vector of finite numbers, with the same length as R
R	(lower bound of the integral) vector of finite positive numbers, with the same length as delta
algo	the algorithm used, 1 or 2

Value

A vector of numbers between 0 and 1, the values of the integral from R to ∞ .

Note

When the number of degrees of freedom is odd, the procedure resorts to the Owen T-function ([OwenT](#)).

References

Owen, D. B. (1965). A special case of a bivariate noncentral t-distribution. *Biometrika* **52**, 437-446.

Examples

```
# OwenQ1(nu, t, delta, R) + OwenQ2(nu, t, delta, R) equals pt(t, nu, delta):
OwenQ1(nu=5, t=3, delta=2, R=1) + OwenQ2(nu=5, t=3, delta=2, R=1)
pt(q=3, df=5, ncp=2)
```

 OwenT

Owen T-function

Description

Evaluates the Owen T-function.

Usage

OwenT(h, a)

Arguments

h	numeric scalar
a	numeric scalar

Details

This is a port of the function `owens_t` of the **boost** collection of C++ libraries.

Value

A number between 0 and 0.25.

References

Owen, D. B. (1956). Tables for computing bivariate normal probabilities. *Ann. Math. Statist.* **27**, 1075-1090.

Examples

```
integrate(function(x) pnorm(1+2*x)^2*dnorm(x), lower=-Inf, upper=Inf)
pnorm(1/sqrt(5)) - 2*OwenT(1/sqrt(5), 1/3)
```

 powen

Owen distribution functions when $\delta_1 > \delta_2$

Description

Evaluates the Owen distribution functions when the noncentrality parameters satisfy $\delta_1 > \delta_2$ and the number of degrees of freedom is integer.

- `powen1` evaluates $P(T_1 \leq t_1, T_2 \leq t_2)$ (Owen's equality 8)
- `powen2` evaluates $P(T_1 \leq t_1, T_2 > t_2)$ (Owen's equality 9)
- `powen3` evaluates $P(T_1 > t_1, T_2 > t_2)$ (Owen's equality 10)
- `powen4` evaluates $P(T_1 > t_1, T_2 \leq t_2)$ (Owen's equality 11)

Usage

```
powen1(nu, t1, t2, delta1, delta2, algo = 2)
```

```
powen2(nu, t1, t2, delta1, delta2, algo = 2)
```

```
powen3(nu, t1, t2, delta1, delta2, algo = 2)
```

```
powen4(nu, t1, t2, delta1, delta2, algo = 2)
```

Arguments

nu	integer greater than 1, the number of degrees of freedom; infinite allowed
t1, t2	two numbers, positive or negative, possible infinite
delta1, delta2	two vectors of possibly infinite numbers with the same length, the noncentrality parameters; must satisfy $\text{delta1} > \text{delta2}$
algo	the algorithm used, 1 or 2

Value

A vector of numbers between 0 and 1, possibly containing some NaN.

Note

When the number of degrees of freedom is odd, the procedure resorts to the Owen T-function ([OwenT](#)).

References

Owen, D. B. (1965). A special case of a bivariate noncentral t-distribution. *Biometrika* **52**, 437-446.

See Also

Use [psbt](#) for general values of delta1 and delta2.

Examples

```
nu=5; t1=2; t2=1; delta1=3; delta2=2
# Wolfram integration gives 0.1394458271284726
( p1 <- powen1(nu, t1, t2, delta1, delta2) )
# Wolfram integration gives 0.0353568969628651
( p2 <- powen2(nu, t1, t2, delta1, delta2) )
# Wolfram integration gives 0.806507459306199
( p3 <- powen3(nu, t1, t2, delta1, delta2) )
# Wolfram integration gives 0.018689824158
( p4 <- powen4(nu, t1, t2, delta1, delta2) )
# the sum should be 1
p1+p2+p3+p4
```

psbt

*Owen distribution functions***Description**

Evaluates the Owen cumulative distribution function for an integer number of degrees of freedom.

- psbt1 evaluates $P(T_1 \leq t_1, T_2 \leq t_2)$
- psbt2 evaluates $P(T_1 \leq t_1, T_2 > t_2)$
- psbt3 evaluates $P(T_1 > t_1, T_2 > t_2)$
- psbt4 evaluates $P(T_1 > t_1, T_2 \leq t_2)$

Usage

```
psbt1(nu, t1, t2, delta1, delta2, algo = 2)
```

```
psbt2(nu, t1, t2, delta1, delta2, algo = 2)
```

```
psbt3(nu, t1, t2, delta1, delta2, algo = 2)
```

```
psbt4(nu, t1, t2, delta1, delta2, algo = 2)
```

Arguments

nu	integer greater than 1, the number of degrees of freedom; infinite allowed
t1, t2	two numbers, positive or negative, possibly infinite
delta1, delta2	two vectors of possibly infinite numbers with the same length, the noncentrality parameters
algo	the algorithm used, 1 or 2

Value

A vector of numbers between 0 and 1, possibly containing some NaN.

Note

When the number of degrees of freedom is odd, the procedure resorts to the Owen T-function ([OwenT](#)).

References

Owen, D. B. (1965). A special case of a bivariate noncentral t-distribution. *Biometrika* **52**, 437-446.

See Also

It is better to use [powen](#) if `delta1 > delta2`.

Examples

```

nu=5; t1=1; t2=2; delta1=2; delta2=3
( p1 <- psbt1(nu, t1, t2, delta1, delta2) )
( p2 <- psbt2(nu, t1, t2, delta1, delta2) )
( p3 <- psbt3(nu, t1, t2, delta1, delta2) )
( p4 <- psbt4(nu, t1, t2, delta1, delta2) )
# the sum should be 1
p1+p2+p3+p4

```

ptOwen

Student CDF with integer number of degrees of freedom

Description

Cumulative distribution function of the noncentral Student distribution with an integer number of degrees of freedom.

Usage

```
ptOwen(q, nu, delta = 0)
```

Arguments

q	quantile, a finite number
nu	integer greater than 1, the number of degrees of freedom; possibly infinite
delta	numeric vector of noncentrality parameters; possibly infinite

Value

Numeric vector, the CDF evaluated at q.

Note

The results are theoretically exact when the number of degrees of freedom is even. When odd, the procedure resorts to the Owen T-function.

References

Owen, D. B. (1965). A special case of a bivariate noncentral t-distribution. *Biometrika* **52**, 437-446.

Examples

```

ptOwen(2, 3) - pt(2, 3)
ptOwen(2, 3, delta=1) - pt(2, 3, ncp=1)

```

`spowen2`*Special case of second Owen distribution function*

Description

Evaluation of the second Owen distribution function in a special case (see details).

Usage

```
spowen2(nu, t, delta, algo = 2)
```

Arguments

<code>nu</code>	positive integer, possibly infinite
<code>t</code>	positive number
<code>delta</code>	vector of positive numbers
<code>algo</code>	the algorithm used, 1 or 2

Details

The value of `spowen2(nu, t, delta)` is the same as the value of `powen2(nu, t, -t, delta, -delta)`, but it is evaluated more efficiently.

Value

A vector of numbers between 0 and 1.

See Also

[powen2](#)

Examples

```
spowen2(4, 1, 2) == powen2(4, 1, -1, 2, -2)
```


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